

# Cryptography

## ECE5632 - Spring 2026

### Lecture 3A

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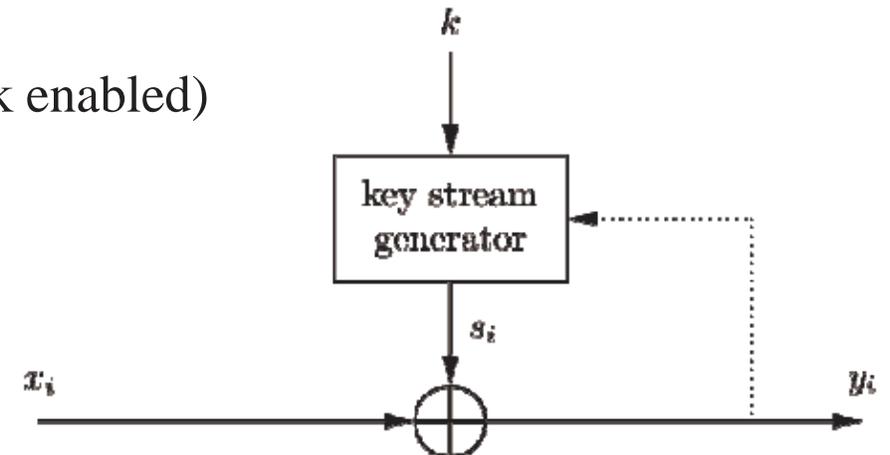


# Lecture Topic

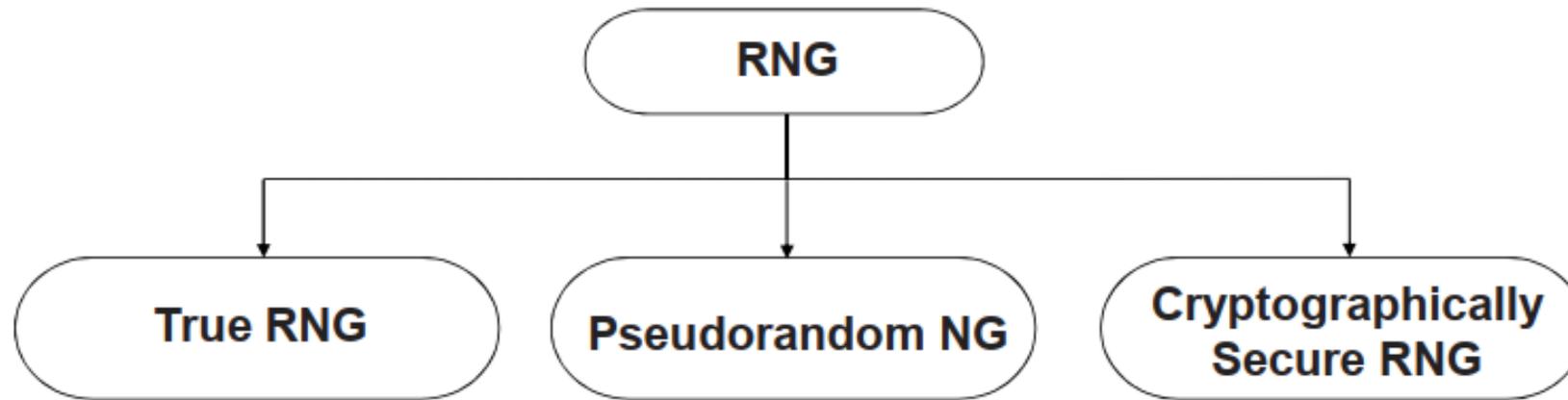
# Stream and Block Ciphers

# Synchronous vs. Asynchronous Stream Cipher

- **Security of stream cipher depends entirely on the key stream  $s_i$ :**
  - Should be **random** , i.e.,  $\Pr(s_i = 0) = \Pr(s_i = 1) = 0.5 = 50\%$
  - Must be **reproducible** by sender and receiver
- **Synchronous Stream Cipher**
  - Key stream depend only on the key (and possibly an initialization vector )
- **Asynchronous Stream Ciphers**
  - Key stream depends also on the ciphertext (dotted feedback enabled)



# Random number generators (RNGs)



## Types of RNGs

- a. True Random Number Generators (TRNG)
- b. Pseudorandom Number Generators (PRNG)
- c. Cryptographically Secure Pseudorandom Number Generators (CSPRNG)

# True Random Number Generators (TRNG)

- Based on physical random processes:  
Some examples: coin flipping, dice rolling, semiconductor noise, radioactive decay, air turbulence, thermal noise, mouse movement, clock jitter of digital circuits.
- Output stream  $si$  should have good statistical properties:  
 $\Pr(si = 0) = \Pr(si = 1) = 50\%$  (often achieved by post-processing)
- Output can neither be predicted nor be reproduced
- Typically used for generation of keys, nonces (used only-once values) and for many other purposes
- Problem: Truly random, i.e., cannot be recreated



# Pseudorandom Number Generator (PRNG)

- Generate sequences from initial seed value
  - Typically, output stream has good statistical properties (meaning their output approximates a sequence of true random numbers).
  - Output can be reproduced and can be predicted
- PRNs are computed, i.e., they are deterministic. Often computed in a recursive way:

$$s_0 = \textit{seed}$$

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$a, b, m$  are integer constants

$$s_{i+1} = f(s_i, s_{i-1}, \dots, s_{i-t})$$

$$s_{i+1} \equiv a s_i + b \pmod{m}, \quad i = 0, 1, \dots$$

- Note that PRNGs are not random in a true sense because they can be computed and are thus completely deterministic.
- A widely used

Example: *rand()* function in ANSI C:

$$s_0 = 12345$$

$$s_{i+1} = 1103515245s_i + 12345 \pmod{2^{31}}$$

❖ Most PRNGs have bad cryptographic properties!

# Cryptographically Secure Pseudorandom Number Generators (CSPRNG)

- CSPRNGs are a special type of PRNG.
- PRNGs with an additional property:
  - Output must be **unpredictable**
- **More precisely:** Given  $n$  consecutive bits of output  $s_i$ , the following output bits  $s_{n+1}$  cannot be predicted (in polynomial time).  
i.e, given  $n$  output bits of the key stream  $s_i, s_{i+1}, \dots, s_{i+n-1}$   
it is computationally infeasible to compute the subsequent bits  $s_{i+n}, s_{i+n+1}, \dots$
- No polynomial time algorithm that can predict the next bit  $s_{n+1}$  with better than 50% chance of success.
- Needed in cryptography, in particular for stream ciphers
- Remark: There are almost no other applications that need unpredictability, whereas many (technical) systems need PRNGs.



# Unconditional Security

**A cipher (cryptosystem) is unconditionally or information-theoretically secure if it cannot be broken even with infinite computational resources.**



# One-Time Pad (OTP)

A stream cipher for which:

- 1) Key stream  $s_0, s_1, s_2, \dots$  is generated by a TRNG.
- 2) Every key stream bit  $s_i$  is only used once.
- 3) Key stream is only known to the legitimate communicating parties.

$$\text{Encryption:} \quad e_{k_i}(x_i) = x_i \oplus k_i$$

$$\text{Decryption:} \quad d_{k_i}(y_i) = y_i \oplus k_i$$

❖ **OTP is unconditionally secure if and only if the key  $k_i$  is used once!**



# One-Time Pad (OTP)

➤ For every ciphertext bit we get an equation of this form :

Unconditionally secure cryptosystem:

$$y_0 = x_0 \oplus k_0$$

$$y_1 = x_1 \oplus k_1$$

:

Every equation is a linear equation with two unknowns

⇒ for every  $y_i$  are  $x_i = 0$  and  $x_i = 1$  equiprobable!

⇒ This is true iff  $k_0, k_1, \dots$  are independent, i.e., all  $k_i$  have to be generated truly random

⇒ It can be shown that this systems can *provably* not be solved.



# Drawbacks of OTP

## 1. Key generation:

a) Obtaining a TRNG is difficult (but doable).

b) Single use means the key is as long as the message, and can't be reused. Very impractical. e.g., For encryption of a 400 MB file, we'd need  $8 \cdot 400 = 3.2$  Gbit of key. Can't be reused for another file.

## 2. Key distribution becomes very complicated, with very large keys that can't be reused and must be eventually destroyed.

❖ For almost all applications the OTP is **impractical** since the key must be as long as the message! (Imagine you have to encrypt a 1GByte email attachment.)



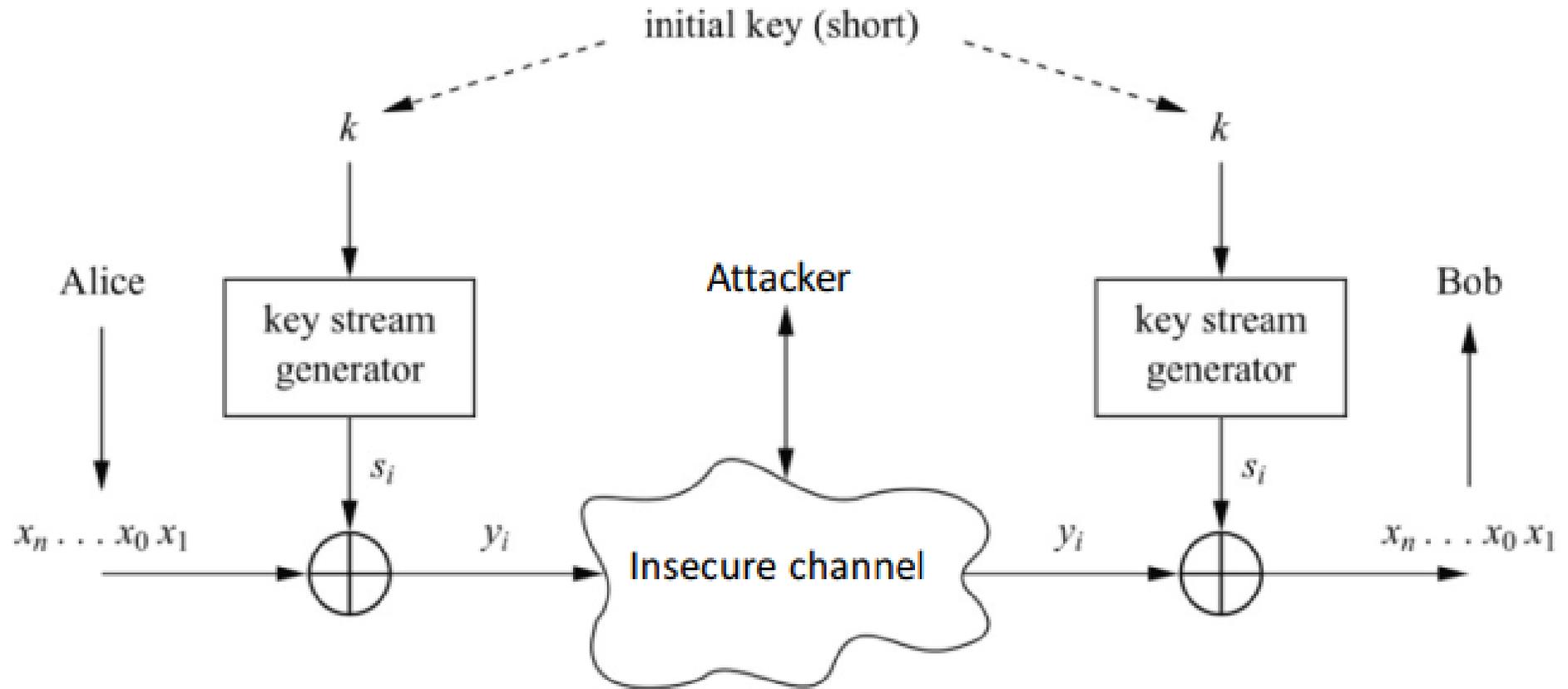
# Computational Security

A cipher is computationally secure if it meets one or both of the following criteria:

- The cost of breaking the cipher exceeds the value of the encrypted information.
- The time required to break the cipher exceeds the useful lifetime of the information.



# Practical Stream Ciphers

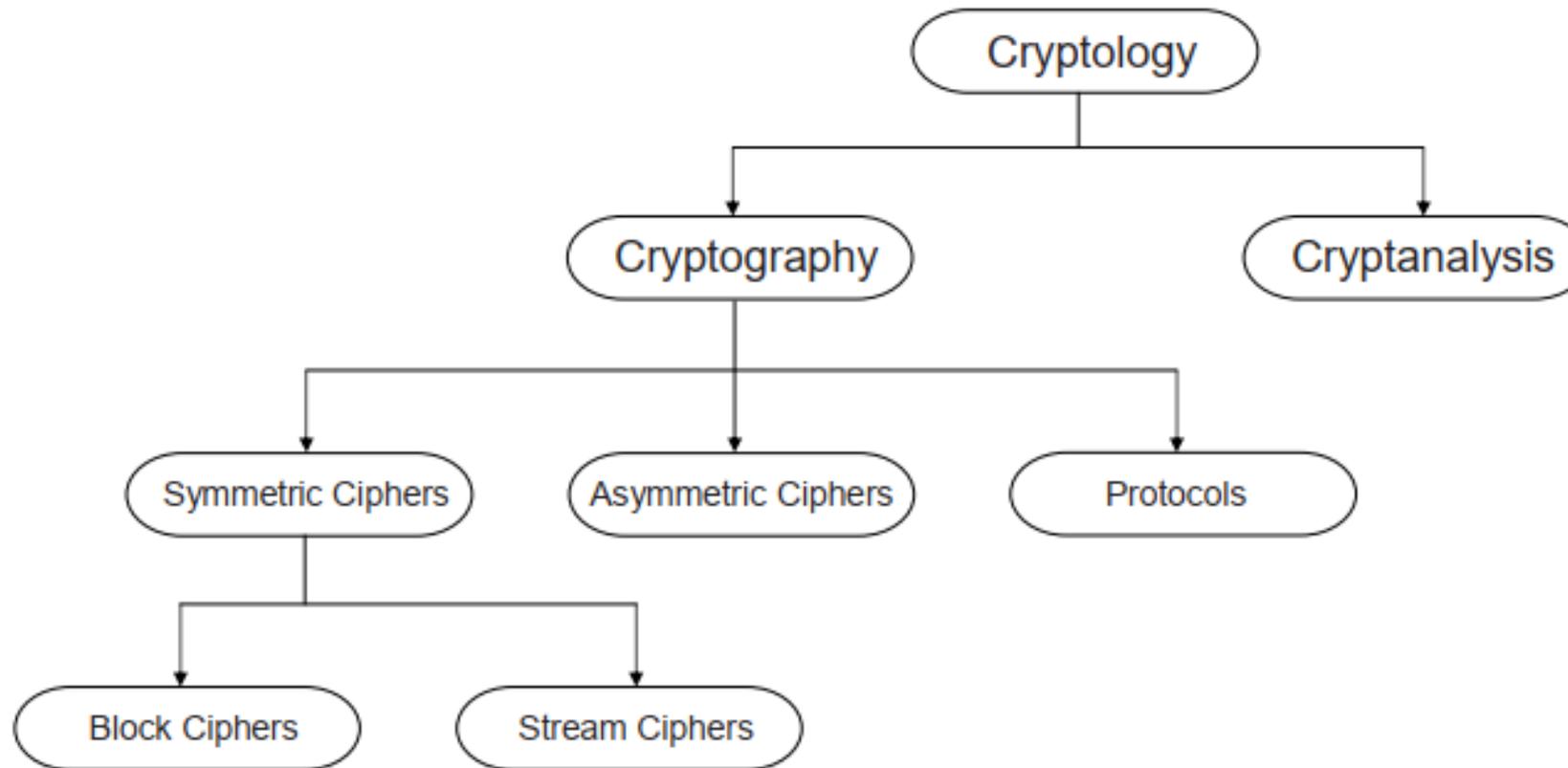


# Practical Stream Ciphers

- Get key streams from PRNGs:
  - e.g., Using linear feedback shift registers (LFSR). Not cryptographically secure.
- Get key streams from CSPRNGs:
  - Using combinations of several LFSRs and nonlinear components.
  - Using block ciphers as building blocks.



# Main Areas of Cryptography



 **You are here!**



# Block Ciphers

- *Simplified Data Encryption Standard (SDES)*
- *Data Encryption Standard (DES)*
- *Advanced Encryption Standard (AES)*



# Strong Block Encryption

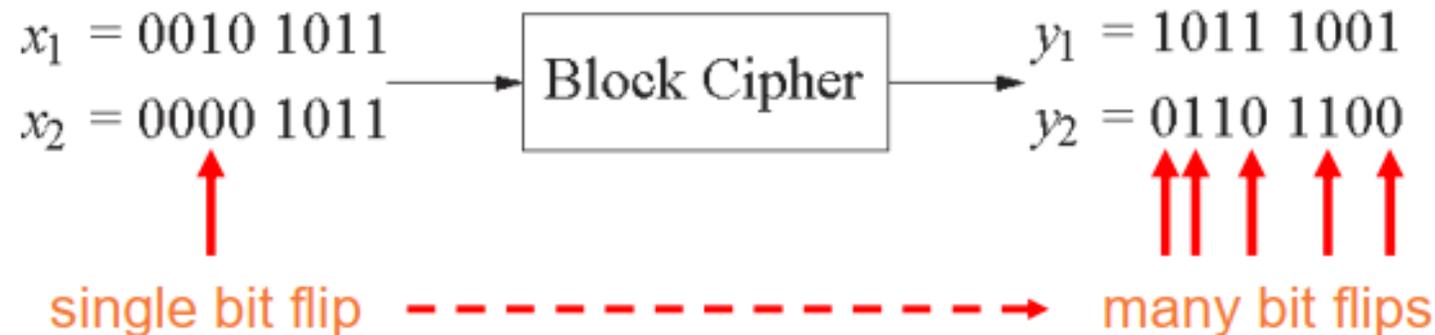
- In 1945, Claude Shannon defined two basic operations to achieve strong encryption:
  - **Confusion:** an encryption operation where the relationship between key and ciphertext is hidden.  
Today, a common element for achieving confusion is **substitution**, which is found in DES
  - **Diffusion:** an encryption operation where the influence of one plaintext bit is spread over many ciphertext bits. with the goal of hiding statistical properties of the plaintext.  
A simple diffusion element is the **bit permutation**, which is frequently used within DES.
- Both operations by themselves cannot provide security. The idea is to concatenate confusion and diffusion elements to build so called *product ciphers*



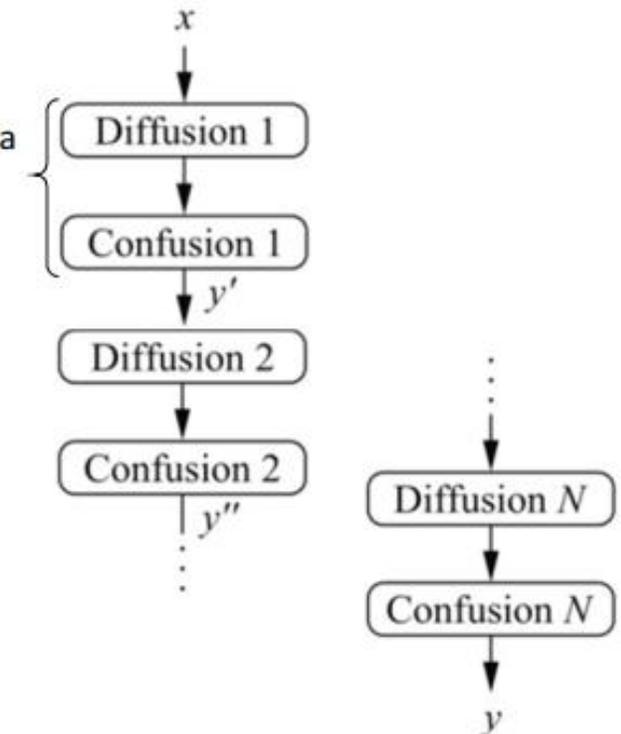
# Product Ciphers

- Most of today's block ciphers are *product ciphers* as they consist of rounds which are applied repeatedly to the data.
- Can reach excellent diffusion: **changing of one bit of plaintext results *on average* in the change of half the output bits.**

**Example:** Let's assume a small block cipher with a block length of 8 bits. Encryption of two plaintexts  $x_1$  and  $x_2$ , which differ only by one bit, should roughly result in something as shown :



Each round performs a confusion and diffusion operation.



"Principle of an N-round product cipher"





# Thank You!

**See You next Lectures!!**  
**Any Question?**

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