# Cryptography ECE 5632 Sheet 4

Spring 2024

#### Problem 1

Compute A(x) + B(x) and A(x).B(x) in  $GF(2^4)$ :

(a) 
$$A(x) = x^2 + 1$$
,  $B(x) = x + 1$ 

(b) 
$$A(x) = x^2 + 1$$
,  $B(x) = x^3 + x^2 + 1$ 

Where, the irreducible polynomial is  $P(x) = x^4 + x + 1$ 

# Problem 2

How many bytes in State are affected by ShiftRows? Describe MixColumns.

## Problem 3

Calculate the first round key  $(K_1)$  of the key expansion for a 128-bit key of all zeros.

## Problem 4

Assume that the input state to the MixColumn layer is [25, 25, ..., 25]. Determine the output.

Note: the MixColumn transformation matrix is :  $\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix}$ 

		у															
		0	1	2	3	4	5	6	7	8	9	A	В	С	D	Е	F
x	0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
	1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
	2	B7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
	3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
	4	09	83	2C	1A	1B	6E	5A	<b>A</b> 0	52	3B	D6	В3	29	E3	2F	84
	5	53	D1	00	ED	20	FC	B1	5B	6A	СВ	BE	39	4A	4C	58	CF
	6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
	7	51	A3	40	8F	92	9D	38	F5	ВС	В6	DA	21	10	FF	F3	D2
	8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
	9	60	81	4F	DC	22	2A	90	88	46	EE	В8	14	DE	5E	0B	DB
	Α	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
	В	E7	C8	37	6D	8D	D5	4E	<b>A</b> 9	6C	56	F4	EA	65	7A	AE	08
	С	BA	78	25	2E	1C	<b>A</b> 6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
	D	70	3E	B5	66	48	03	F6	0E	61	35	57	В9	86	C1	1D	9E
	Е	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
	F	8C	<b>A</b> 1	89	0D	BF	E6	42	68	41	99	2D	0F	В0	54	BB	16

(a) S-box

Figure 1: S-Box